

ITAP - Osnove uporabe R

A. Blejec

andrej.blejec@nib.si

Nacionalni inštitut za biologijo
in
Univerza v Ljubljani
BF Oddelek za biologijo

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Normalna porazdelitev

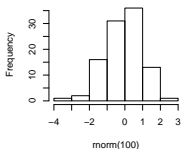
```
> rnorm(5)      # 5 slučajnih števil iz  $N(0, 1)$   
[1] -1.19142464  0.54930055 -0.06240514  0.26544150  
[5] -0.23459751  
  
> args(rnorm)  # kakšni so argumenti funkcije rnorm?  
function (n, mean = 0, sd = 1)  
NULL
```

```

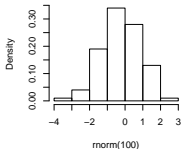
> oldpar <- par (mfrow = c(2, 2)) # pripravi štiri panel
> hist(rnorm(100))                # histogram 100 slučaj
> hist(rnorm(100), prob = T)      # verjetnosti na ordin
> hist(rnorm(100, 50, 10))        # argumenti po vrsti:
> hist(rnorm(100, sd = 10, mean = 50), prob = T) # druga
> par (oldpar)                    # privzemi prejšnje vr

```

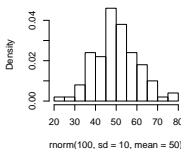
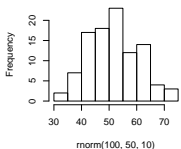
Histogram of rnorm(100)



Histogram of rnorm(100)



Histogram of rnorm(100, 50, 10) histogram of rnorm(100, sd = 10, mean



Funkcije za verjetnostne porazdelitve

<u>Distribution</u>	<u>R name</u>	<u>additional arguments</u>
beta	<code>beta</code>	<code>shape1, shape2, ncp</code>
binomial	<code>binom</code>	<code>size, prob</code>
Cauchy	<code>cauchy</code>	<code>location, scale</code>
chi-squared	<code>chisq</code>	<code>df, ncp</code>
exponential	<code>exp</code>	<code>rate</code>
F	<code>f</code>	<code>df1, df2, ncp</code>
gamma	<code>gamma</code>	<code>shape, scale</code>
geometric	<code>geom</code>	<code>prob</code>
hypergeometric	<code>hyper</code>	<code>m, n, k</code>
log-normal	<code>lnorm</code>	<code>meanlog, sdlog</code>
logistic	<code>logis</code>	<code>location, scale</code>
negative binomial	<code>nbinom</code>	<code>size, prob</code>
normal	<code>norm</code>	<code>mean, sd</code>
Poisson	<code>pois</code>	<code>lambda</code>
Student's t	<code>t</code>	<code>df, ncp</code>
uniform	<code>unif</code>	<code>min, max</code>
Weibull	<code>weibull</code>	<code>shape, scale</code>
Wilcoxon	<code>wilcox</code>	<code>m, n</code>

Funkcije za verjetnostne porazdelitve

Predpone

random	slučajna števila	<code>rnorm(n, ...)</code>
density	gostota verjetnosti	<code>dnorm(x, ...)</code>
probability	kvantilni rang	<code>pnorm(q, ...)</code>
qantile	kvantil	<code>qnorm(p, ...)</code>

```
> oldopts <- options(digits=3)
```

```
> rnorm(5)
```

```
[1] -1.270 -0.371  0.389 -1.431 -2.503
```

```
> dnorm(seq(-3, 2, 1))
```

```
[1] 0.00443 0.05399 0.24197 0.39894 0.24197 0.05399
```

```
> pnorm(1.96)
```

```
[1] 0.975
```

```
> qnorm(0.975)
```

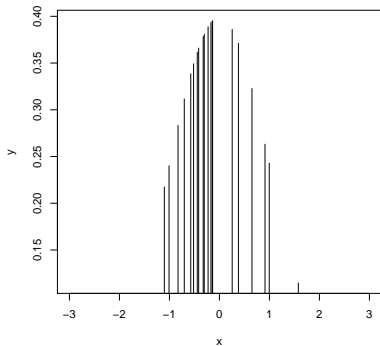
```
[1] 1.96
```

Slika verjetij

```
> slVer <- function(n=20,m=1,xlim=c(-3,3)) {  
+ for(j in 1:m)  
+ {  
+ x <- rnorm(n)  
+ y <- dnorm(x)  
+ plot(x,y,type="h",xlim=xlim)  
+ }  
+ }  
> slVer()
```

Slika verjetij

```
> slVer()
```

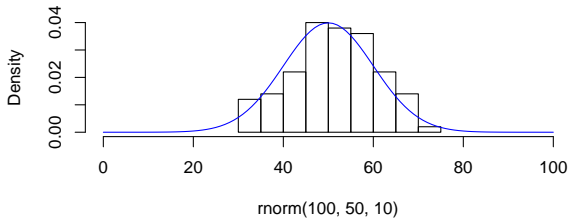


Funkcije za verjetnostne porazdelitve

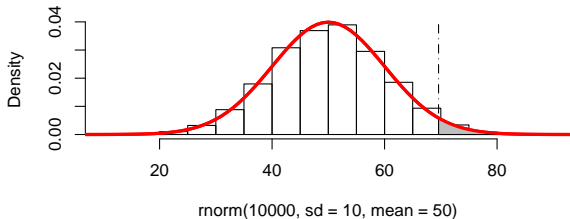
```
> oldpar <- par (mfrow = c(2, 1))
> hist(rnorm(100, 50,10), prob = T, xlim = c(0, 100))
> lines(0:100, dnorm(0:100, 50, 10), col = "blue", xpd=TRUE)
> hist(rnorm(10000, sd = 10, mean = 50), prob = T) # za
> lines(0:100, dnorm(0:100, 50, 10), col = "red", lwd =
> (q <- qnorm(.975, 50, 10)) # kv
> abline (v = qnorm(.975, 50, 10), lty = "1373") # doda
> #
> # pobarvaj kritični del porazdelitve
> #
> px <- seq(q, 100) # prip
> py <- c(dnorm(px, 50, 10))
> polygon(c(px, q), c(py, 0), col = 8) # poba
> lines(0:100, dnorm(0:100, 50, 10), col = "red", lwd =
> par (oldpar)
```


Funkcije za verjetnostne porazdelitve

Histogram of `rnorm(100, 50, 10)`



Histogram of `rnorm(10000, sd = 10, mean = 50)`



Simulacija linearne regresije:

$$Y = 2X + 3 + \varepsilon \quad X \sim N(20, 5) \text{ in } \varepsilon \sim N(0, 10)$$

```
> n=20
> x <- round(rnorm(n, 20, 5)) #
> mean(x)

[1] 20.85

> var(x)                # var računa nepristransko varianco !!

[1] 32.23947

> x

[1] 18 25 23 26 20 15 28 24 20 25 29 17 11 15 28 15 21
[18] 12 17 28

> y <- 2*x+3            # izračunaj ustrezne y
```

Simulacija linearne regresije:

$$Y = 2X + 3 + \varepsilon \quad X \sim N(20, 5) \text{ in } \varepsilon \sim N(0, 10)$$

```
> mean(y)                # preveri parametre y
[1] 44.7

> var(y)
[1] 128.9579

> mean(x) * 2 + 3
[1] 44.7

> var(x) * 4
[1] 128.9579

> eps <- round(rnorm(n, sd=10)) # Pa še eps, mean=0
> mean(eps)
[1] -0.35

> var(eps)
[1] 119.7132
```

Simulacija linearne regresije:

$$Y = 2X + 3 + \varepsilon \quad X \sim N(20, 5) \text{ in } \varepsilon \sim N(0, 10)$$

```
> Y <- y+eps      # sestavi obe slučajni spremenljivki
> Y

 [1] 22 58 62 63 35 35 82 35 57 36 67 48 22 27 50 31 43
[18] 27 38 49

> var(Y)          # Ali veljajo lastnosti za varianco vs
[1] 271.3974

> var(y)+var(eps) # videti je, da sta Y in eps koreliran
[1] 248.6711

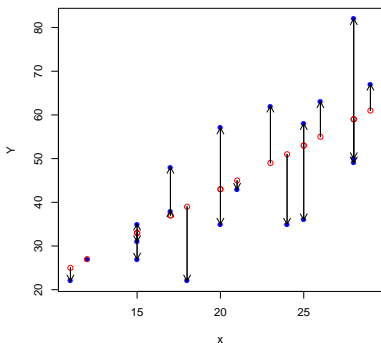
> cor(y, eps)     # !!
[1] 0.0914543

> var(y)+var(eps)+2*cov(y, eps)      # zdaj pa bo
[1] 271.3974
```

Simulacija linearne regresije:

$$Y = 2X + 3 + \varepsilon \quad X \sim N(20, 5) \text{ in } \varepsilon \sim N(0, 10)$$

- > `plot(x, Y, col="blue", pch=16)` # korelacijski grafikon za
- > `points(x, y, col="red")` # modelirane točke x, y
- > `segments(x, y, x, Y)` # odkloni (ε)
- > `arrows(x, y, x, Y, length=.1)` # podobno, a s puščicami



Simulacija linearne regresije:

$$Y = 2X + 3 + \varepsilon \quad X \sim N(20, 5) \text{ in } \varepsilon \sim N(0, 10)$$

```
> fit<-lsfit(x,Y)           # "least squares fit"  
> names(fit)
```

```
[1] "coefficients" "residuals"      "intercept"  
[4] "qr"
```

```
> fit$coefficients
```

```
Intercept      X  
-1.024406    2.176231
```

```
> yHat<-cbind(1,x)%%fit$coeff
```

Linerana regresija: $Y = 2x + 3 + \varepsilon$: $x \sim N(20, 5)$ in $\varepsilon \sim N(0, 10)$

```
> plot(x, Y, col="blue", pch=16) # korelacijski grafikon za  
> points(x, y, col="red")      # modelirane točke x, y  
> segments(x, y, x, Y)        # odkloni (eps)  
> arrows(x, y, x, Y, length=.1) # podobno, a s puščicami  
> abline(lsfit(x, Y))         # dodaj regresijsko črto  
> abline(lsfit(x, Y), col=3, lwd=3) # malo jo olepšaj  
> points(x, yHat)
```

